

BIG BANG NUCLEOSYNTHESIS

Theoretical estimation of primordial abundances and comparison with current observations

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Outline

- Nuclear Statistical Equilibrium (NSE)

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- Initial Conditions

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- BBN step by step

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- BBN as a constraint for new physics
- Summary

Nuclear Statistical Equilibrium (NSE)

Kinetic equilibrium among the light nuclear species:

$$n_A = g_A \left(\frac{m_A T}{2\pi} \right)^{3/2} \exp \left\{ \frac{\mu_A - m_A}{T} \right\} \quad (1)$$

Nucleus A is produced out of Z protons and (A-Z) neutrons, If $(A - Z)n + Zp \rightarrow A$ occurs rapidly compared to the expansion rate, chemical equilibrium is attained:

$$\mu_A = Z\mu_p + (A - Z)\mu_n$$

Regarding the definition of the binding energy :

$$B_A = m_A - (A - Z)m_n - Zm_p$$

$$n_A = g_A A^{3/2} 2^{-A} \left(\frac{2\pi}{m_N T} \right)^{3(A-1)/2} n_p^Z n_n^{A-Z} \exp\{B_A/T\} \quad (2)$$

Some binding energies

$Z A$	B_A [MeV]	g_A
${}^2\text{H}$	2.22	3
${}^3\text{H}$	6.92	2
${}^3\text{He}$	7.72	2
${}^4\text{He}$	28.3	1
${}^{12}\text{C}$	92.2	1

Nucleon density:

$$n_N = n_n + n_p + \sum_i (A n_A)_i$$

Abundances

$$X_A = \frac{A n_A}{n_N}$$

$$\sum_i X_i = 1$$

Using $\eta \equiv n_N/n_\gamma = 2.68 \cdot 10^{-8}(\Omega_B h^2)$ The abundance of specie A is:

$$X_A = g_A [\zeta(3)^{(A-1)} \pi^{(1-A)/2} 2^{3(A-1)/2}] A^{5/2} (T/m_N)^{3(A-1)/2} \\ \times \eta^{(A-1)} X_p^Z X_n^{(A-Z)} \exp\{B_A/T\}$$

Initial Conditions ($T \gg 1 \text{ MeV}$, $t \ll 1 \text{ s}$)

At this stage the proton-neutron balance is maintained through:

Chemical equilibrium maintained for slow expansion!



$$\mu_n + \mu_\nu = \mu_p + \mu_e$$

In thermal equilibrium:

$$n/p \equiv \frac{n_n}{n_p} = \frac{X_n}{X_p} = \exp\{-Q/T + (\mu_e - \mu_\nu)/T\}$$

$$Q \equiv m_n - m_p = 1.293 \text{ MeV}$$

How to estimate $(\mu_e - \mu_\nu)$?

$$\mu_e/T \sim (n_e/n_\gamma) = (n_p/n_\gamma) = \eta \sim 10^{-10} \quad \text{Negligible!}$$

↑ Charge neutrality of the universe

What about μ_ν/T ?

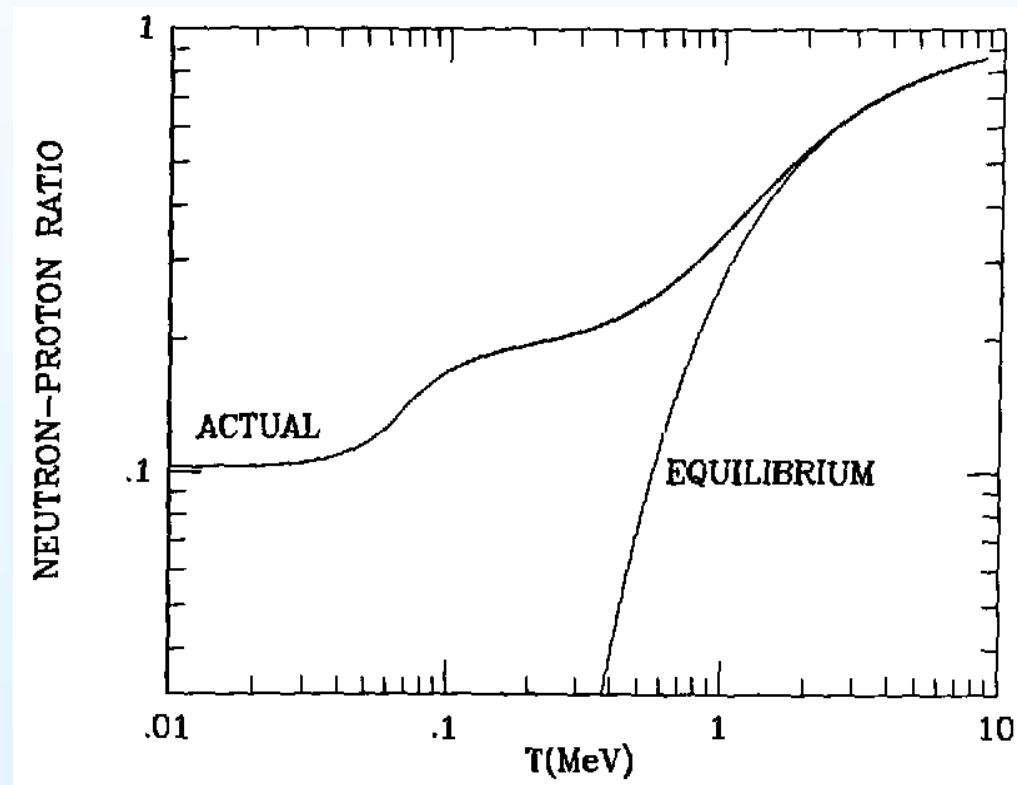
$$\mu_{\nu e}/T \sim (n_{\nu e}/n_\gamma)$$

- Neutrino background have not yet been measured
- None of the neutrino lepton numbers is known
- Assume they are small $\Rightarrow |\mu_{\nu e}|/T \ll 1$
- This term might be of relevance in non standard BBN scenarios!

Under the last assumption:

$$\left(\frac{n}{p}\right)_{\text{EQ}} = \exp\{-Q/T\}$$

Kolb, Turner; The Early Universe:
n-p ratio as function of temperature.



Weak Rates and Neutrino freeze-out Temperature

$$\Gamma_{pe \rightarrow \nu n} = \int f_e(E_e)[1 - f_\nu(E_\nu)] |\mathcal{M}|^2 \delta^4(p + e - n - \nu) \\ \times \frac{d^3 p_e}{2E_e} \frac{d^3 p_n}{2E_n} \frac{d^3 p_\nu}{2E_\nu}$$

β decay matrix element:

$$|\mathcal{M}|^2 \propto G_F^2 (1 + 3g_A^2); \quad g_A \simeq 1.26$$

Related to the unweighted neutron decay rate:

$$\tau_n^{-1} = \Gamma_{n \rightarrow pe\nu} = \frac{G_F^2}{2\pi^3} (1 + 3g_A^2) m_e^5 \lambda_0; \quad \lambda_0 = 1.636$$

Using the above result:

$$\Gamma_{pe \rightarrow \nu n} = (\tau_n \lambda_0)^{-1} \int_q^\infty d\epsilon \frac{\epsilon(\epsilon - q)^2(\epsilon^2 - 1)^{1/2}}{[1 + \exp\{\epsilon z\}][1 + \exp\{(q - \epsilon)z_\nu\}]}$$

$$q = Q/m_e \quad \epsilon = E_e/m_e \quad z = m_e/T \quad z_\nu = m_e/T_\nu$$

Identical procedures can be applied to obtain $\Gamma_{n \rightarrow pe\nu}$ (weighted), $\Gamma_{ne \rightarrow p\nu}$, $\Gamma_{n\nu \rightarrow pe}$, $\Gamma_{pe\nu \rightarrow n}$, $\Gamma_{p\nu \rightarrow ne}$ and $\Gamma_{pe \rightarrow n\nu}$.

Group them:

$$\Gamma_n = \Gamma_{n \rightarrow pe\nu} + \Gamma_{ne \rightarrow p\nu} + \Gamma_{n\nu \rightarrow pe} = (\tau_n \lambda_0)^{-1} \lambda_n$$

$$\Gamma_p = \Gamma_{pe\nu \rightarrow n} + \Gamma_{p\nu \rightarrow ne} + \Gamma_{pe \rightarrow n\nu} = (\tau_n \lambda_0)^{-1} \lambda_p$$

neutron and proton number densities determined by Boltzmann eqns.:

$$\dot{n}_n + 3Hn_n = (\tau_n \lambda_0)^{-1} [\lambda_p n_p - \lambda_n n_n]$$

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...computer code required...However, for $T \geq m_e \Rightarrow \Gamma_p \simeq G_F^2 T^5$.

$$H = 1.66 g_*^{1/2} T^2 / m_p l, g_* = 10.75:$$

$$\Gamma_p / H \sim (T / 0.8 \text{ MeV})^3$$

Since $e^+ + e^- \leftrightarrow \nu + \bar{\nu}$ has a smaller cross section
 $T_F = 0.8 \text{ MeV}$ is the neutrino freeze-out temperature!

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- **What about other nuclear species at $T \sim 1 \text{ MeV}$?**
Nuclear reactions that build up the light nuclei are faster than the expansion rate \Rightarrow NSE abundances should occur!

Playing with NSE abundances

The toys: neutrons, protons, D (**2**), ³He (**3**), ⁴He (**4**), ¹²C (**12**)
(Some heavy nucleus).

The rules:

$$X_n = X_p \exp\{-Q/T\}$$

$$X_2 = 16.3(T/m_N)^{3/2}\eta \exp\{B_2/T\}X_pX_n$$

$$X_3 = 57.4(T/m_N)^3\eta^2 \exp\{B_3/T\}X_p^2X_n$$

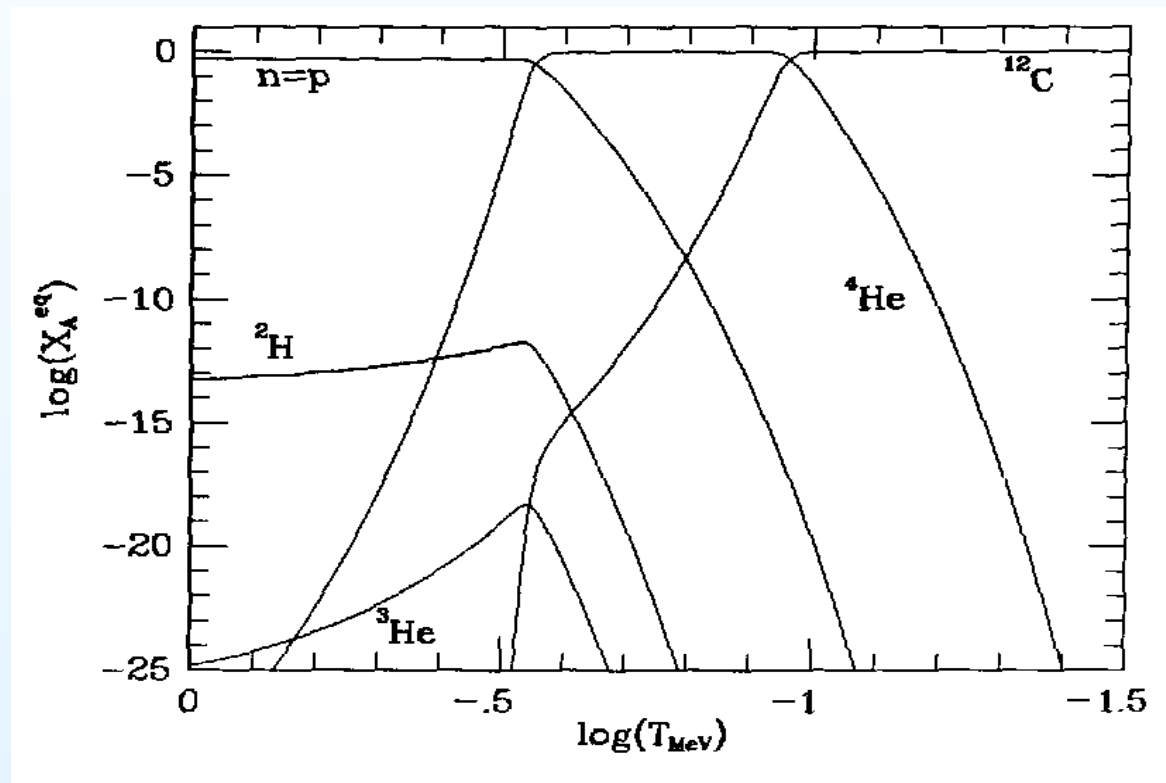
$$X_4 = 113(T/m_N)^{9/2}\eta^4 \exp\{B_4/T\}X_p^2X_n^2$$

$$X_{12} = 3.22 \cdot 10^5 (T/m_N)^{33/2}\eta^{11} \exp\{B_{12}/T\}X_p^6X_n^6$$

$$X_p + X_n + X_2 + X_3 + X_4 + X_{12} = 1$$

When a specie A is thermally favored?

Kolb, Turner; The Early Universe:
NSE abundances ($X_n = X_p$).



No significant fractions are produced before neutrino freeze out!

BBN Step by Step I ($t \simeq 10^{-2}$ s, $T \simeq 10$ MeV)

- Radiation dominated universe:

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- Light elements are in NSE, but η so small \Rightarrow small abundances

$$X_n = X_p \simeq 0.5 \quad X_2 \simeq 6 \cdot 10^{-12} \quad X_3 \simeq 2 \cdot 10^{-23} \quad X_4 \simeq 2 \cdot 10^{-34}$$

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As T decreases (n/p) is reduced by neutron decays.
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- NSE abundances, but still very small!

$$X_n \simeq 1/7 \quad X_p \simeq 6/7 \quad X_2 \simeq 10^{-12} \quad X_3 \simeq 10^{-23} \quad X_4 \simeq 10^{-28}$$

BBN Step by Step III ($t \simeq 1 - 3$ min, $T \simeq 0.3 - 0.1$ MeV)

- For $T \simeq m_e/3$, e^\pm annihilation occurs \Rightarrow Reheating $(T/T_\nu) = (11/4)^{1/3}$.

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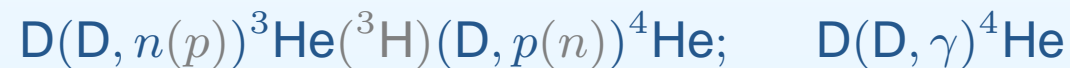
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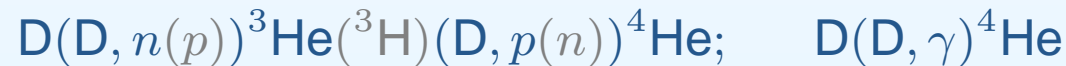
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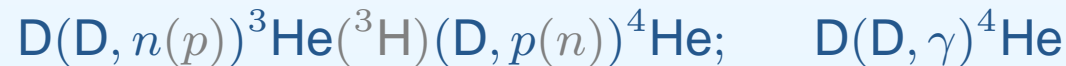
- D, ${}^3\text{He}$ and ${}^3\text{H}$ abundances begin to exceed their NSE values, but still small.

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- T decreasing \Rightarrow Significant Coulomb Barrier suppression!

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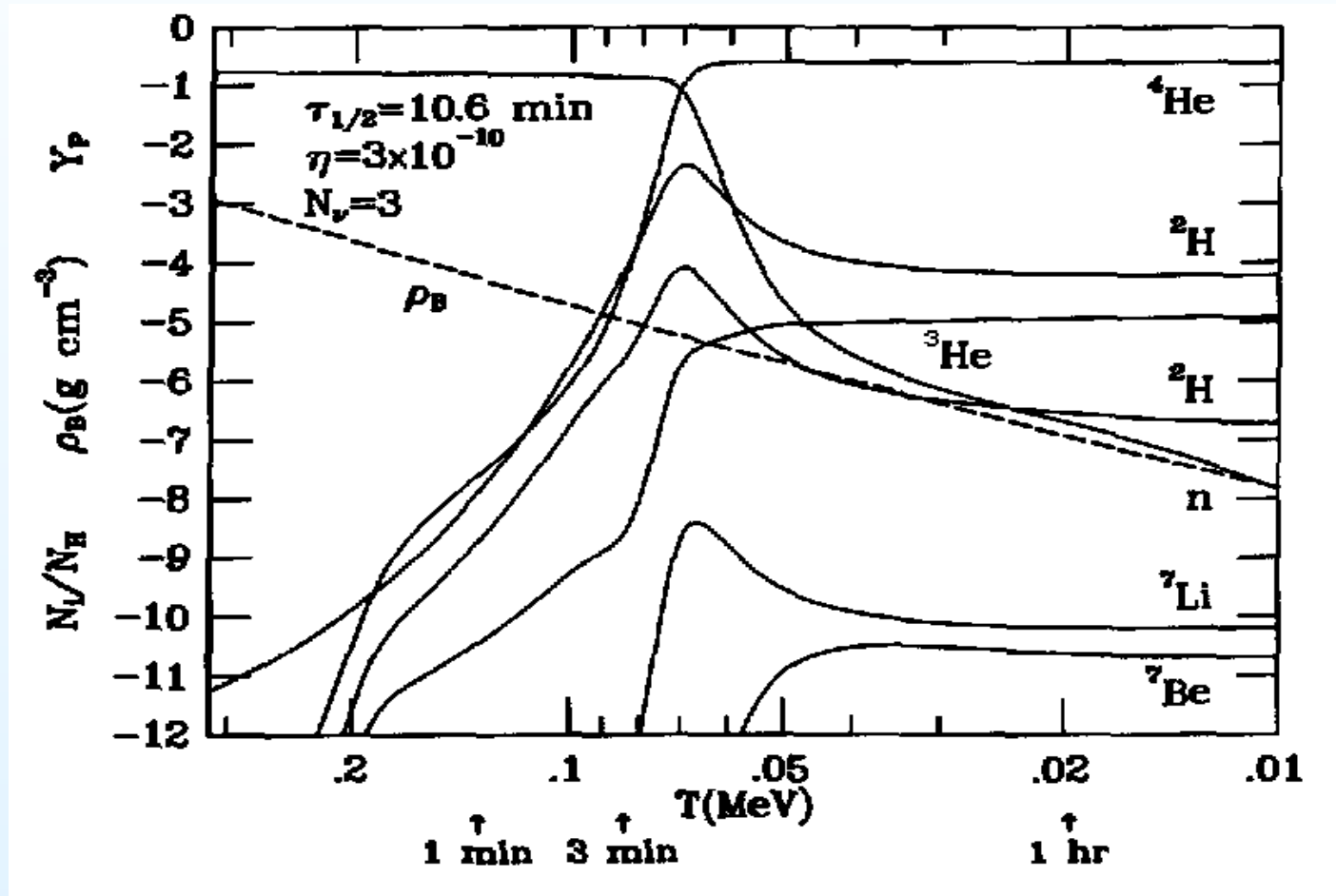
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 - Rates proportional to $\eta \Rightarrow$ abundances should decrease with increasing η .

Standard BBN Predictions

- Necessity of a computer code

Kolb, Turner; The Early Universe: The development of BBN.



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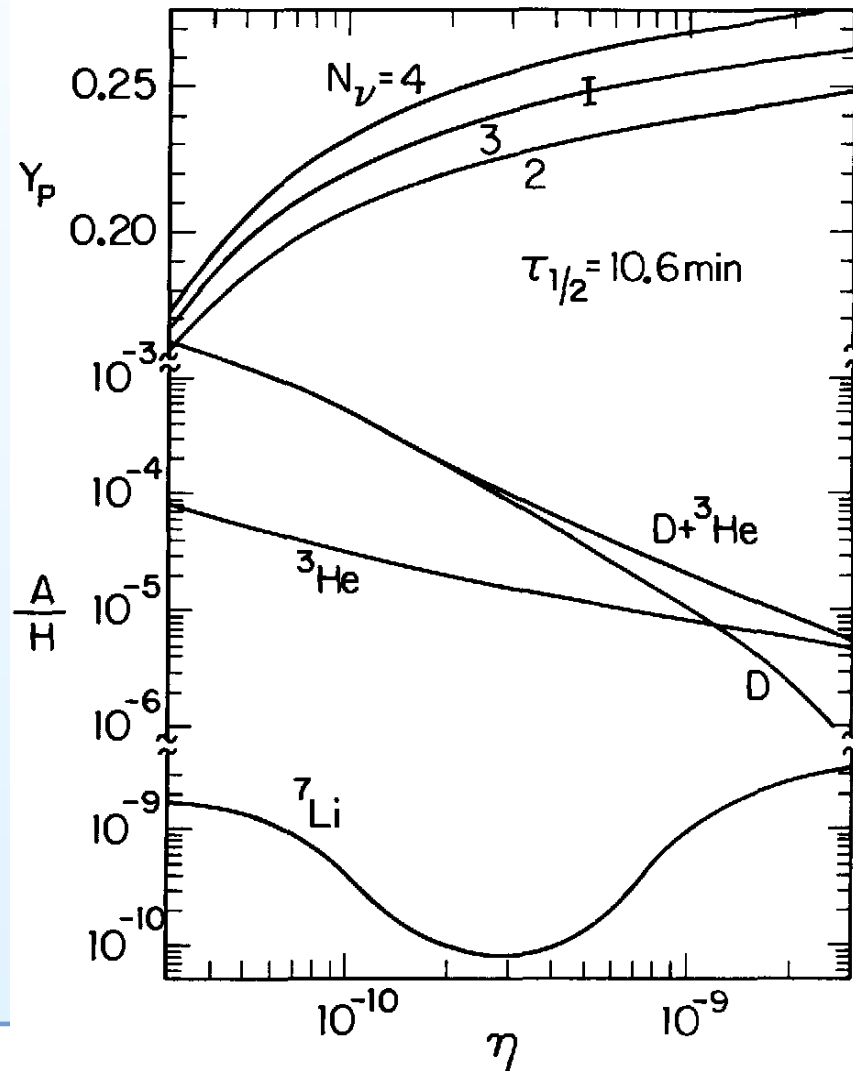
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 - $g_*(T_F)$ plays an important role in determination of the freeze out temperature.

Kolb, Turner; The Early Universe: BBN abundances vs. η .



- $\tau_{1/2}: \Gamma \propto T^5 / \tau_{1/2} \Rightarrow T_F \propto \tau_{1/2}^{1/3}$
- $g_*: H \propto g_*^{1/2} T^2 \Rightarrow T_F \propto g_*^{1/6}$
- $\eta: X_A \propto \eta^{(A-1)}$

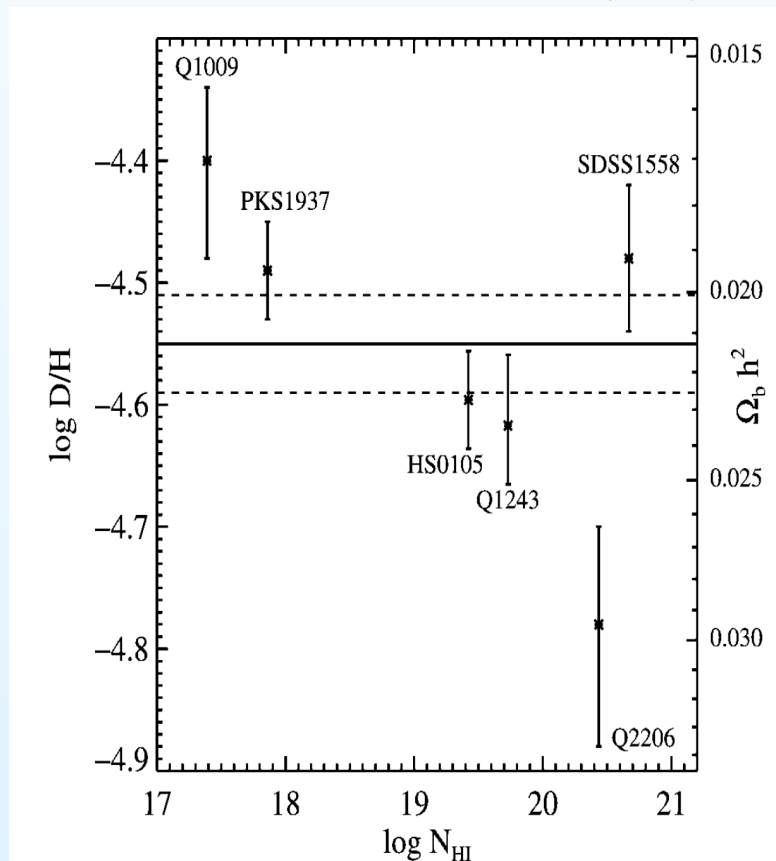
Primordial Abundance Observations

...Stars do not help

- Deuterium

J.M. O'Meara *et al.*, *Astrophys. J. Lett.* **649**, L61 (2006).

The best measurements of $(D/H)_P$.



- Deuterium is not efficiently produced in stellar processes.
- Any abundance measurement imposes a lower bound on $(D/H)_P \Rightarrow$ upper bound on η
- D presence is revealed by high-resolution spectra of high-red shift low-metallicity absorption quasars.
- Astration may have reduced galactic ISM by a factor of 1.12 ± 0.13 .
- Average of the six most accurate abundances in quasar systems:

$$(D/H)_P = (2.82 \pm 0.12[1\sigma] \{0.21[3\sigma]\}) \cdot 10^{-5}$$

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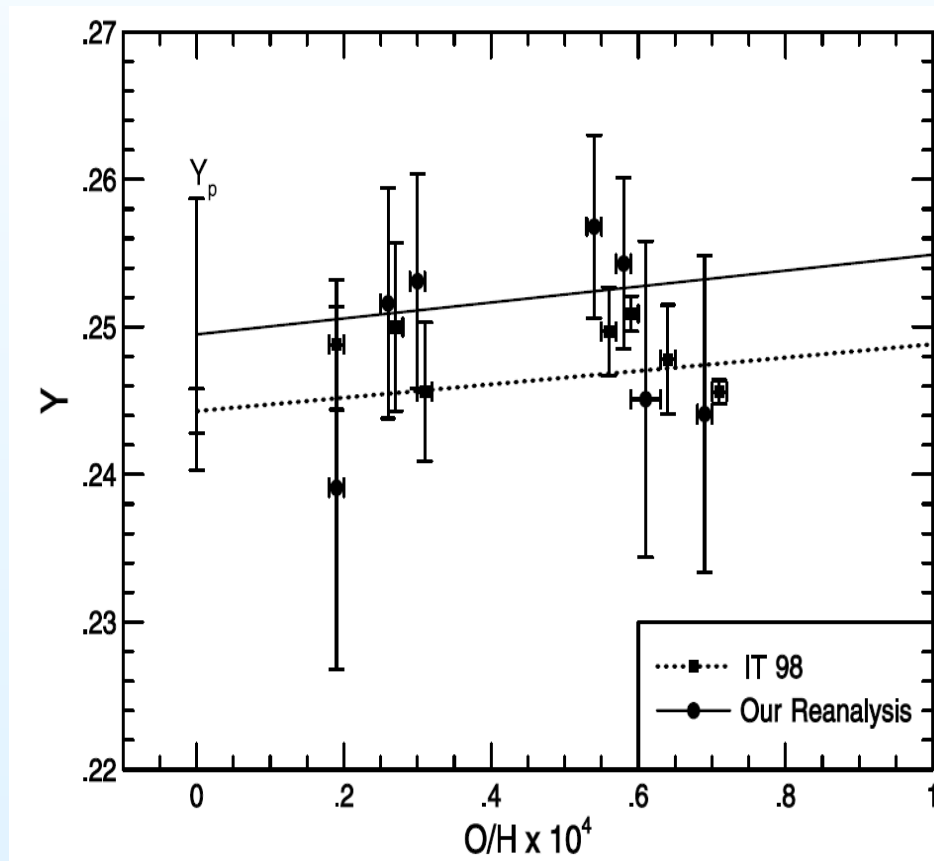
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- Just a bound:

$$\left(\frac{\text{D} + {}^3\text{He}}{\text{H}}\right)_{\text{P}} \leq 8 \cdot 10^{-5} \quad \Rightarrow \quad \eta \geq 4 \cdot 10^{-10}$$

- ${}^4\text{He}$

K.A. Olive & E. Skillman, *Astrophys. J.* **617**, 29 (2004).
Helium abundance vs. Metallicity.



- Measurement of recombination lines in HII galactic and extragalactic regions.
- Correlation between metallicity and ${}^4\text{He}$ abundance.
- Extrapolate to zero metallicity:

$$Y_{\text{p}} = 0.249 \pm 0.009$$

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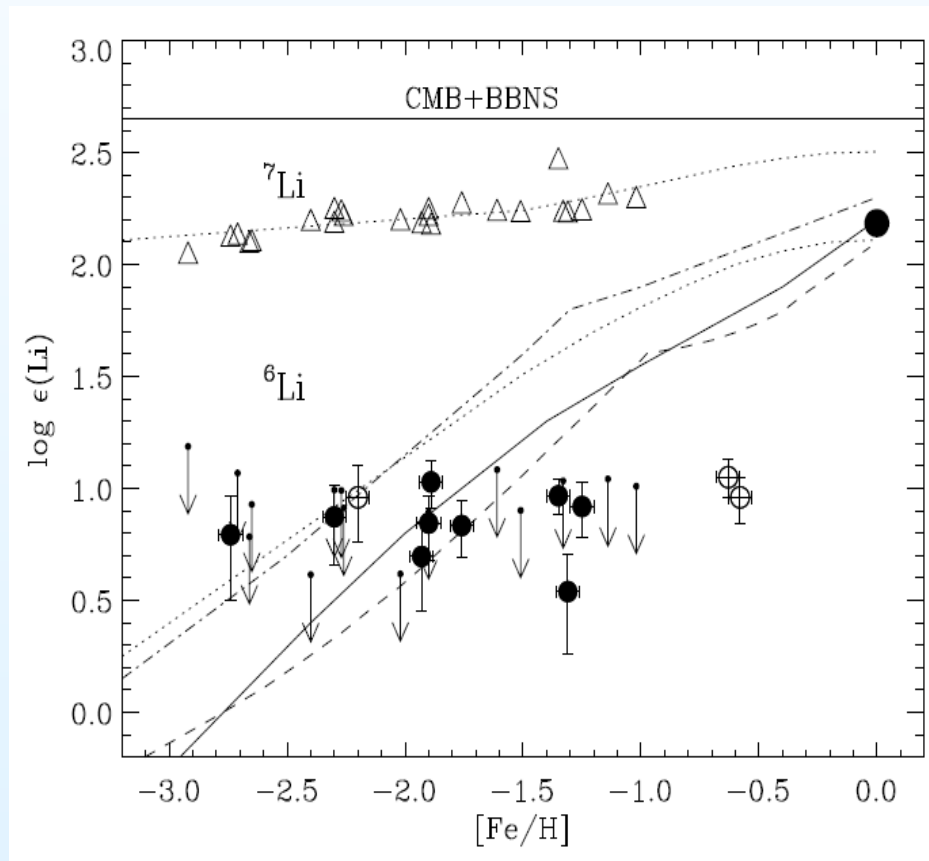
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- From the plateau: $({}^7\text{Li}/\text{H})_{\text{P}} = (1.7 \pm 0.06 \pm 0.44) \cdot 10^{-10}$

- Evidence for primordial ${}^6\text{Li}$?

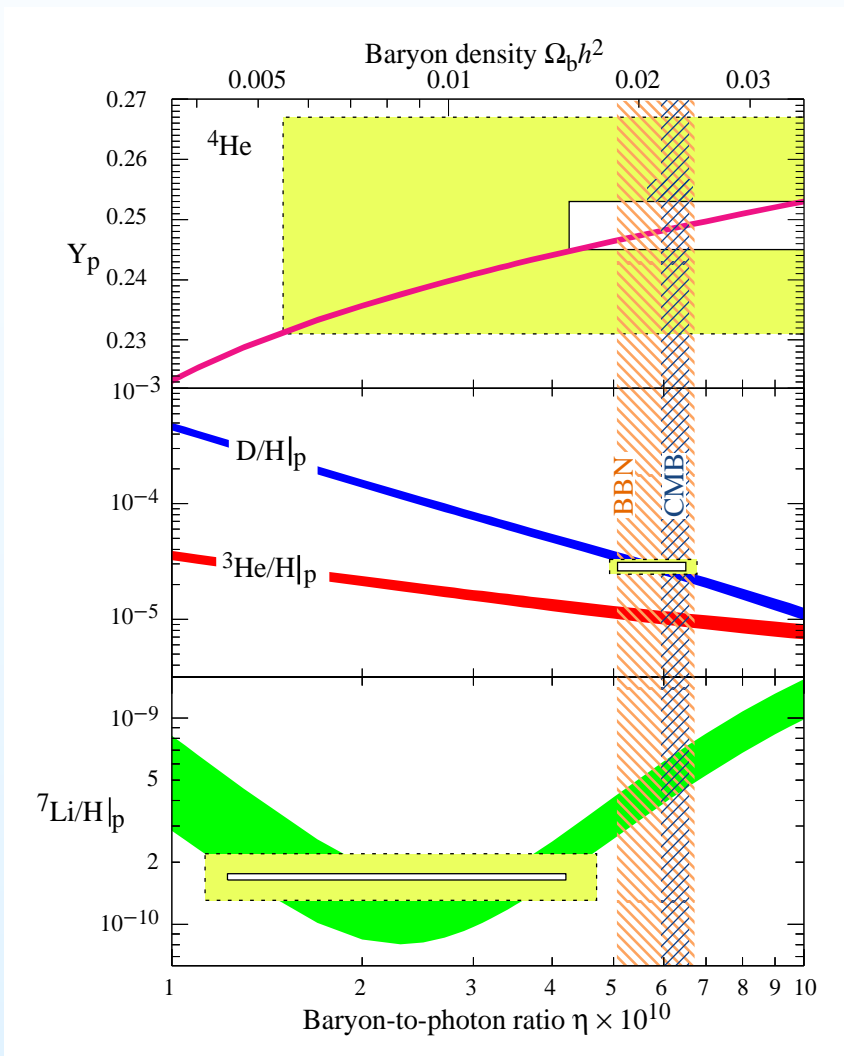
M. Asplund *et al.*, *Astrophys. J.* **644**, 229 (2006).
Spite plateau for lithium isotopes.



- Current spectral resolution permits to determine the isotopic fraction in Pop II stars:

$$\frac{{}^6\text{Li}}{{}^7\text{Li}} \leq 0.15$$

- Spite plateau is also observed for ${}^6\text{Li}$.
- Can be generated by convection processes.
- The plateau is interpreted as an upper bound for primordial ${}^6\text{Li}$.



Amsler *et al.* (PDG), Phys. Lett. **B667**, 1 (2008).
 Theory and Observation altogether

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- Consistency between current measurements and SBBN necessarily forces one (maybe two) Lithium problem.
- $(\text{H}/\text{D})_{\text{p}}$ agreement with CMB values for the baryon density.
- Extensions of SM have to explain ^7Li (^6Li) primordial abundance and predict abundances for ^4He and D in agreement with SBBN.

References

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